

COMMON MULTIPLES OF PATH, STAR AND CYCLE WITH  
COMPLETE BIPARTITE GRAPHS

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(Received: Apr. 10, 2021 Accepted: Apr. 06, 2022 Published: Apr. 30, 2022)

**Abstract:** A graph  $G$  is a common multiple of two graphs  $H_1$  and  $H_2$  if there exists a decomposition of  $G$  into edge-disjoint copies of  $H_1$  and also a decomposition of  $G$  into edge-disjoint copies of  $H_2$ . If  $G$  is a common multiple of  $H_1$  and  $H_2$ , and  $G$  has  $q$  edges, then we call  $G$  a  $(q, H_1, H_2)$  graph. Our paper deals with the following question: Given two graphs  $H_1$  and  $H_2$ , for which values of  $q$  does there exist a  $(q, H_1, H_2)$  graph? when  $H_1$  is either a path or a star or a cycle and  $H_2$  is a complete bipartite graph.

**Keywords and Phrases:** Graph Decomposition, Common Multiples of Graphs, Path, Star, Cycle, Complete Bipartite Graph.

**2020 Mathematics Subject Classification:** 05C38, 05C51, 05C70.

## 1. Introduction

All graphs considered here are finite and undirected unless otherwise noted. Let  $|V(G)|$  and  $e(G)$  denote, respectively, the order of a graph  $G$  and the size of  $G$ , that is, the number of edges in  $G$ .

$K_n$  denotes the complete graph on  $n$  vertices, and  $K_{m,n}$  denotes the complete bipartite graph with vertex partitions of cardinality  $m$  and  $n$ . A  $k$ -path, denoted