

**ESTIMATES OF INITIAL COEFFICIENTS FOR FUNCTIONS IN  
NEW SUBCLASSES OF BI-UNIVALENT FUNCTIONS DEFINED  
USING GENERALIZED DIFFERENTIAL OPERATOR**

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(Received: Mar. 03, 2020 Accepted: April. 26, 2020 Published: Apr. 30, 2020)

**Abstract:** We defined a new subclass of the function class  $\Sigma$  in the unit disk associated with a generalized differential operator. We estimated some coefficient bounds for the functions in the defined new subclass. As special cases, well-known results were obtained by varying parameters in the main results.

**Keywords and Phrases:** Coefficient bounds, bi-univalent, subclasses, differential operator.

**2010 Mathematics Subject Classification:** Primary 30C45, secondary 30C50.

**1. Introduction and Preliminaries**

We denote by  $A$  the class of regular functions defined in the open unit disk  $\Delta = \{z : |z| < 1\}$  with the normalization conditions  $f(0) = f'(0) - 1 = 0$  and the Taylor series expansion,

$$f(z) = z + \sum_{k=2}^{\infty} a_k z^k \tag{1}$$

We know that "The range of every function of the class  $S$  contains a disk  $\{w : |w| < 1/4\}$ ", by the Koebe-one quater theorem [3] (Theorem 2.3 pg. 31). Hence there exists inverse  $f^{-1}$  for every function  $f \in S$ , defined by  $f^{-1}(f(z)) = z, (z \in \Delta)$  and

$$f(f^{-1}(w)) = w, (|w| < r_0(f) : r_0(f) \geq 1/4).$$